|  | Lesson | Standards for a Geometry Course | Pacing |
| :---: | :---: | :---: | :---: |
| Unit 1 ESSENTIALS OF GEOMETRY |  |  |  |
| Module 1: Geometry in the Plane |  |  |  |
| 1.1 | Points, Lines, and Planes | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). | 2 days |
| 1.2 | Define and Measure Angles | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). | 2 days |
| 1.3 | Polygons and Other Figures in the Plane | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. | 2 days |
| $1.4$ | Apply the Distance Formula | Use coordinates to prove simple geometric theorems algebraically. <br> Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.* <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* | 2 days |
| Module 2: Tools for Reasoning and Proof |  |  |  |
| $2.1$ | Write Conditional Statements | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. | 1 day |
| 2.2 | Use Inductive and Deductive Reasoning | Prove geometric theorems about lines and angles. | 2 days |
| 2.3 | Write Proofs about Segments | Prove geometric theorems about lines and angles. | 2 days |
| 2.4 | Write Proofs about Angles | Prove geometric theorems about lines and angles. | 2 days |
| Unit 2 PARALLEL AND PERPENDICULAR LINES |  |  |  |
| Module 3: Lines and Transversals |  |  |  |
| 3.1 | Parallel Lines Crossed by a Transversal | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Prove geometric theorems about lines and angles. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). | 1 day |

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| 3.2 | Prove Lines Are Parallel | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Prove geometric theorems about lines and angles. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). | 2 days |
| 3.3 | Prove Lines Are Perpendicular | Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Prove geometric theorems about lines and angles. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). | 2 days |
| Module 4: Lines on the Coordinate Plane |  |  |  |
| 4.1 | Slope and Equations of Parallel Lines | Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | 2 days |
| 4.2 | Slope and Equations of Perpendicular Lines | Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | 2 days |
| 4.3 | Write a Coordinate Proof | Use coordinates to prove simple geometric theorems algebraically. | 2 days |
| Unit 3 TRANSFORMATIONS |  |  |  |
| Module 5: Transformations that Preserve Size and Shape |  |  |  |
| 5.1 | Define and Apply Translations | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. <br> Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. <br> Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | 1 day |


|  | Lesson | Standards for a Geometry Course | Pacing |
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| 5.2 | Define and Apply Rotations | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. <br> Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. <br> Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | 1 day |
| 5.3 | Define and Apply Reflections | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. <br> Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. <br> Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | 1 day |
| 5.4 | Define and Apply Symmetry | Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. | 2 days |
| Module 6: Transformations that Change Size and Shape |  |  |  |
| 6.1 | Define and Apply Dilations, Stretches, and Compressions | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Verify experimentally the properties of dilations given by a center and a scale factor: <br> - A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged. <br> - The dilation of a line segment is longer or shorter in the ratio given by the scale factor. | 2 days |

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| 6.2 | Apply Sequences of Transformations | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. <br> Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. <br> Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | 1 day |
| Unit 4 TRIANGLE CONGRUENCE |  |  |  |
| Module 7: Congruent Triangles and Polygons |  |  |  |
| 7.1 | Understand Congruent Figures | Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent. | 1 day |
| 7.2 | Corresponding Parts of Congruent Figures | Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent. | 1 day |
| 7.3 | Use Rigid Motions to Prove Figures Are Congruent | Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. <br> Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent. | 2 days |
| Module 8: Triangle Congruence Criteria |  |  |  |
| 8.1 | Develop ASA Triangle Congruence | Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |
| 8.2 | Develop SAS Triangle Congruence | Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |
| 8.3 | Develop SSS Triangle Congruence | Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |

"One day" is equal to one instructional period in a traditional schedule and would

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| 8.4 | Develop AAS and HL <br> Triangle Congruence | Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |
| Unit 5 RELATIONSHIPS WITHIN TRIANGLES |  |  |  |
| Module 9: Properties of Triangles |  |  |  |
| $9.1$ | Angle Relationships in Triangles | Prove theorems about triangles. <br> Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle. | 1 day |
| 9.2 | Perpendicular Bisectors in Triangles | Prove theorems about triangles. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). <br> Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. | 2 days |
| 9.3 | Angle Bisectors in Triangles | Prove theorems about triangles. <br> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometry software, etc.). <br> Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. | 2 days |
| 9.4 | Medians and Altitudes in Triangles | Prove theorems about triangles. <br> Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. | 2 days |
| $9.5$ | The Triangle Midsegment Theorem | Prove theorems about triangles. | 1 day |
| Module 10: Triangle Inequalities |  |  |  |
| 10.1 | Inequalities Within a Triangle | Prove theorems about triangles. <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* | 1 day |
| $10.2$ | Inequalities Between Two Triangles | Prove theorems about triangles. <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* | 1 day |
| Unit 6 QUADRILATERALS, POLYGONS, AND TRIANGLE SIMILARITY |  |  |  |
| Module 11: Quadrilaterals and Polygons |  |  |  |
| 11.1 | Properties of Parallelograms | Prove theorems about parallelograms. <br> Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. | 2 days |


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| 11.2 | Conditions for Parallelograms | Prove theorems about parallelograms. <br> Use coordinates to prove simple geometric theorems algebraically. <br> Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | 2 days |
| 11.3 | Properties of Rectangles, Rhombuses, and Squares | Prove theorems about parallelograms. <br> Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. | 2 days |
| 11.4 | Conditions for Rectangles, Rhombuses, and Squares | Prove theorems about parallelograms. <br> Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle. <br> Use coordinates to prove simple geometric theorems algebraically. <br> Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | 2 days |
| 11.5 | Properties and Conditions for Trapezoids and Kites | Prove theorems about parallelograms. <br> Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. <br> Use coordinates to prove simple geometric theorems algebraically. <br> Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | 2 days |
| Module 12: Similarity |  |  |  |
| 12.1 | Use Transformations to Prove Figures Are Similar | Verify experimentally the properties of dilations given by a center and a scale factor: <br> - A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged. <br> - The dilation of a line segment is longer or shorter in the ratio given by the scale factor. <br> Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding angles and the proportionality of all corresponding pairs of sides. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. <br> Prove that all circles are similar. <br> Find the point on a directed line segment between two given points that partitions the segment in a given ratio. | 2 days |

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| $12.2$ | Develop AA Triangle Similarity | Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar. <br> Prove theorems about triangles. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |
| 12.3 | Develop and Prove Triangle Proportionality | Verify experimentally the properties of dilations given by a center and a scale factor: <br> - A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged. <br> - The dilation of a line segment is longer or shorter in the ratio given by the scale factor. <br> Prove theorems about triangles. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. <br> Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. | 2 days |
|  | Apply Similarity in Right Triangles | Prove theorems about triangles. <br> Use congruence and similarity criteria for triangles to solve problems and prove relationships in geometric figures. | 2 days |
| Unit 7 RIGHT TRIANGLE TRIGONOMETRY |  |  |  |
| Module 13: Trigonometry with Right Triangles |  |  |  |
| 13.1 | Tangent Ratio | Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. <br> Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.* | 2 days |
| 13.2 | Sine and Cosine Ratios | Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. <br> Explain and use the relationship between the sine and cosine of complementary angles. <br> Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.* | 2 days |
| 13.3 | Special Right Triangles | Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. <br> Explain and use the relationship between the sine and cosine of complementary angles. <br> Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.* | 2 days |

[^2]|  | Lesson | Standards for a Geometry Course | Pacing |
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| $13.4$ | Solve Problems Using Trigonometry | Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. <br> Explain and use the relationship between the sine and cosine of complementary angles. <br> Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.* | 2 days |
| Module 14: Trigonometry with All Triangles |  |  |  |
| 14.1 | Law of Sines | Prove the Laws of Sines and Cosines and use them to solve problems. <br> Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces). | 2 days |
| 14.2 | Law of Cosines | Prove the Laws of Sines and Cosines and use them to solve problems. <br> Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces). <br> Derive the formula $A=1 / 2 a b \sin (C)$ for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side. | 2 days |
| Unit 8 PROPERTIES OF CIRCLES |  |  |  |
| Module 15: Angles and Segments in Circles |  |  |  |
| 15.1 | Central Angles and Inscribed Angles | Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. <br> Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. <br> Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. <br> Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle. | 2 days |
| 15.2 | Angles in Inscribed Quadrilaterals | Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. <br> Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. <br> Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle. | 2 days |


|  | Lesson | Standards for a Geometry Course | Pacing |
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| $15.3$ | Tangents and Circumscribed Angles | Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. <br> Construct a tangent line from a point outside a given circle to the circle. | 2 days |
| $15.4$ | Circles on the Coordinate Plane | Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation. <br> Use coordinates to prove simple geometric theorems algebraically. | 2 days |
| Module 16: Relationships in Circles |  |  |  |
| $16.1$ | Segment Relationships in Circles | Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. | 2 days |
| $16.2$ | Angle Relationships in Circles | Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. | 2 days |
| Module 17: Circumference and Area of a Circle |  |  |  |
| 17.1 | Measure Circumference and Area of a Circle | Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments. | 1 day |
| 17.2 | Measure Arc Length and Use Radians | Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector. | 2 days |
| 17.3 | Measure Sector Area | Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector. | 2 days |
| Unit 9 SURFACE AREA AND VOLUME |  |  |  |
| Module 18: Surface Area |  |  |  |
| 18.1 | Three-Dimensional Figures | Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of twodimensional objects. <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 1 day |

In addition to the core instructional pacing below, HMH recommends the following:

- 3 days per year for the Growth Measure assessments
- 2 days per module for the Module Performance Task, Are You Ready?, Module Review, and Module Test - 1 day per unit for the Unit Test

Using these recommendations, the total pacing for Geometry is 180 days.

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| 18.2 | Surface Areas of Prisms and Cylinders | Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 2 days |
| 18.3 | Surface Areas of Pyramids and Cones | Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 2 days |
| 18.4 | Surface Areas of Spheres | Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 2 days |
| Module 19: Volume |  |  |  |
| 19.1 | Volumes of Prisms and Cylinders | Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments. <br> Give an informal argument using Cavalieri's principle for the formulas for the volume of a sphere and other solid figures. <br> Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.* <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 1 day |


| Lesson | Standards for a Geometry Course | Pacing |
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| 19.2 Volumes of Pyramids and Cones | Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments. <br> Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.* <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 2 days |
| 19.3 Volumes of Spheres | Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments. <br> Give an informal argument using Cavalieri's principle for the formulas for the volume of a sphere and other solid figures. <br> Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.* <br> Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).* <br> Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).* <br> Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).* | 2 days |
| Unit 10 PROBABILITY |  |  |
| Module 20: Probability of Multiple Events |  |  |
| 20.1 Probability and Set Theory | Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or,""and," "not").* | 2 days |
| 20.2 Disjoint and Overlapping Events | Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities.* <br> Apply the Addition Rule, $P(A$ or $B)=P(A)+P(B)-P(A$ and $B)$, and interpret the answer in terms of the model.* | 2 days |


| Lesson | Standards for a Geometry Course | Pacing |
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| Module 21: Conditional Probability and Independence of Events |  |  |
| 21.1 Conditional Probability | Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or,""and,""not").* <br> Understand the conditional probability of $A$ given $B$ as $P(A$ and $B) / P(B)$, and interpret independence of $A$ and $B$ as saying that the conditional probability of $A$ given $B$ is the same as the probability of $A$, and the conditional probability of $B$ given $A$ is the same as the probability of $B$.* <br> Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations.* <br> Find the conditional probability of $A$ given $B$ as the fraction of $B^{\prime}$ s outcomes that also belong to $A$, and interpret the answer in terms of the model.* | 2 days |
| 21.2 Independent Events | Understand that two events $A$ and $B$ are independent if the probability of $A$ and $B$ occurring together is the product of their probabilities, and use this characterization to determine if they are independent.* <br> Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations.* | 2 days |
| 21.3 Dependent Events | Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations.* <br> Apply the general Multiplication Rule in a uniform probability model, $P(A$ and $B)=P(A) P(B \mid A)=P(B) P(A \mid B)$, and interpret the answer in terms of the model.* | 2 days |


[^0]:    * This is also a modeling standard.

[^1]:    * This is also a modeling standard.

[^2]:    * This is also a modeling standard.

