## Module 1: Real Numbers and Real-World Quantities

| 1.1 | Real Numbers | Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational. | 1 day |
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| 1.2 | Radicals and Rational Exponents | Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. <br> Rewrite expressions involving radicals and rational exponents using the properties of exponents. | 2 days |
| 1.3 | Precision and Accuracy in Calculations | Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.* | 2 days |
| Module 2: Linear Equations and Inequalities in One Variable |  |  |  |
| 2.1 | Write, Interpret, and Simplify Expressions | Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> - Interpret complicated expressions by viewing one or more of their parts as a single entity. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* | 1 day |
| 2.2 | Write and Solve Equations | Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. <br> Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* | 1 day |

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| 2.3 | Rewrite Formulas and <br> Solve Literal Equations | Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.* <br> Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret complicated expressions by viewing one or more of their parts as a single entity. | 2 days |
| 2.4 | Write and Solve Inequalities | Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. | 1 day |
| 2.5 | Write and Solve Compound Inequalities | Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> - Interpret complicated expressions by viewing one or more of their parts as a single entity. | 2 days |



* This is also a modeling standard.

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| 4.2 | Linear Functions | Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$. The graph of $f$ is the graph of the equation $y=f(x)$. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.* | 2 days |
| 4.3 | Characteristics of Linear Functions | For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. | 2 days |


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| 4.4 Linear Models and PointSlope Form | Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.* | 2 days |
| Module 5: Relationships Among Linear Functions |  |  |
| 5.1 Transform Graphs of Functions | Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* | 2 days |


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| 5.2 Transform Linear Functions | Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. <br> Write a function that describes a relationship between two quantities.* <br> - Combine standard function types using arithmetic operations. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| 5.3 Compare Linear Functions | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 1 day |


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| 5.4 Inverses of Linear Functions | Find inverse functions. <br> - Solve an equation of the form $f(x)=c$ for a simple function $f$ that has an inverse and write an expression for the inverse. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 1 day |
| Unit 3 BUILD LINEAR FUNCTIONS AND MODELS |  |  |
| Module 6: Fit Linear Functions to Data |  |  |
| 6.1 Scatter Plots, Correlation, and Fitted Lines | Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.* <br> - Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models. <br> - Fit a linear function for a scatter plot that suggests a linear association. <br> Distinguish between correlation and causation.* <br> Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.* <br> Interpret the parameters in a linear or exponential function in terms of a context.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |


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| 6.2 | Residuals and Best-Fit Lines | Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.* <br> - Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models. <br> - Informally assess the fit of a function by plotting and analyzing residuals. <br> - Fit a linear function for a scatter plot that suggests a linear association. <br> Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.* <br> Compute (using technology) and interpret the correlation coefficient of a linear fit.* <br> Interpret the parameters in a linear or exponential function in terms of a context.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| Module 7: Discrete Linear Functions |  |  |  |
| 7.1 | Arithmetic Sequences Defined Recursively | Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. <br> Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.* <br> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| 7.2 | Arithmetic Sequences Defined Explicitly | Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. <br> Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.* <br> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

## Module 8: Piecewise-Defined Functions

8.1 Graph Piecewise-Defined Functions

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.*

- Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*
Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*
Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.*
Write a function that describes a relationship between two quantities.*
- Determine an explicit expression, a recursive process, or steps for calculation from a context.

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| 8.2 | Graph Absolute Value Functions | Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. <br> Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| 8.3 | Solve Absolute Value Equations and Inequalities | Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. <br> Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.* <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. | 2 days |

## Module 9: Systems of Linear Equations

9.1 Solve Linear Systems by Graphing
9.3 Solve Linear Systems by Adding or Subtracting

Solve systems of linear equations exactly and approximately (e.g., with graphs), $\quad 1$ day focusing on pairs of linear equations in two variables.

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*
Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.*
Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*

Define appropriate quantities for the purpose of descriptive modeling.*
Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*
Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.*
Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.*

Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.
Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*

Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.*

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
*This is also a modeling standard.

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| 9.4 | Solve Linear Systems by Multiplying First | Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. <br> Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. | 2 days |
| Module 10: Linear Inequalities |  |  |  |
| 10.1 | Linear Inequalities in Two Variables | Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. | 2 days |
| 10.2 | Graph Systems of Linear Inequalities | Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. <br> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* | 2 days |

"One day" is equal to one instructional period in a traditional schedule and would

## Unit 5 EXPONENTIAL FUNCTIONS AND EQUATIONS

Module 11: Exponential Functions and Models
11.1 Exponential Growth Functions

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.*

- Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*

Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).*

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*

Define appropriate quantities for the purpose of descriptive modeling.*
Interpret expressions that represent a quantity in terms of its context.*

- Interpret parts of an expression, such as terms, factors, and coefficients.
- Interpret complicated expressions by viewing one or more of their parts as a single entity.

Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.*

Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.*

Write a function that describes a relationship between two quantities.*

- Determine an explicit expression, a recursive process, or steps for calculation from a context.

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| 11.2 Exponential Decay Functions | Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* <br> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |


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| 11.3 Rewrite Exponential Models | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.* <br> - Use the properties of exponents to transform expressions for exponential functions. <br> Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. <br> - Use the properties of exponents to interpret expressions for exponential functions. <br> Interpret expressions that represent a quantity in terms of its context.* <br> - Interpret parts of an expression, such as terms, factors, and coefficients. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. | 1 day |
| Module 12: Relationships Among Exponential Functions |  |  |
| 12.1 Transform Exponential Functions | Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. <br> Write a function that describes a relationship between two quantities.* <br> - Combine standard function types using arithmetic operations. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude. <br> Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. <br> Interpret expressions that represent a quantity in terms of a context.* <br> - Interpret complicated expressions by viewing one or more of their parts as a single entity. | 2 days |

In addition to the core instructional pacing below, HMH recommends the following: - 3 days per year for the Growth Measure assessments

- 2 days per module for the Module Performance Task, Are You Ready?, Module Review, and Module Test - 1 day per unit for the Unit Test

Using these recommendations, the total pacing for Algebra 1 is 177 days.

| Lesson | Standards for an Algebra 1 Course | Pacing |
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| 12.2 Compare Exponential Functions | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <br> Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.* <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude. <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

## Unit 6 BUILD EXPONENTIAL FUNCTIONS AND MODELS

Module 13: Fit Exponential Functions to Data
13.1 Scatter Plots and Fitted Exponential Curves

Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.*

- Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
- Informally assess the fit of a function by plotting and analyzing residuals.

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*

Distinguish between situations that can be modeled with linear functions and with exponential functions.*

- Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.*

- Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
- Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

Write a function that describes a relationship between two quantities.*

- Determine an explicit expression, a recursive process, or steps for calculation from a context.

Interpret the parameters in a linear or exponential function in terms of a context.*

In addition to the core instructional pacing below, HMH recommends the following: - 3 days per year for the Growth Measure assessments

- 2 days per module for the Module Performance Task, Are You Ready?, Module Review, and Module Test - 1 day per unit for the Unit Test

Using these recommendations, the total pacing for Algebra 1 is 177 days.

| Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: |
| 13.2 Choose Between Linear and Exponential Models | Distinguish between situations that can be modeled with linear functions and with exponential functions.* <br> - Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. <br> - Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. <br> - Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another. <br> Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.* <br> - Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models. <br> - Fit a linear function for a scatter plot that suggests a linear association. <br> Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. <br> Interpret the parameters in a linear or exponential function in terms of a context.* | 2 days |

$\left.\begin{array}{|l|l|l|l|}\hline \mathbf{1 4 . 1} \begin{array}{l}\text { Geometric Sequences } \\ \text { Defined Recursively }\end{array} & \begin{array}{l}\text { Recognize that sequences are functions, sometimes defined recursively, whose } \\ \text { domain is a subset of the integers. } \\ \text { Write arithmetic and geometric sequences both recursively and with an explicit } \\ \text { formula, use them to model situations, and translate between the two forms.* } \\ \text { Construct linear and exponential functions, including arithmetic and geometric } \\ \text { sequences, given a graph, a description of a relationship, or two input-output } \\ \text { pairs (include reading these from a table).* } \\ \text { Use units as a way to understand problems and to guide the solution of multi- } \\ \text { step problems; choose and interpret units consistently in formulas; choose and } \\ \text { interpret the scale and the origin in graphs and data displays.* } \\ \text { Define appropriate quantities for the purpose of descriptive modeling.* }\end{array} & 2 \text { days }\end{array}\right\}$

## Unit 7 POLYNOMIAL OPERATIONS AND MODELS

## Module 15: Polynomial Multiplication

15.1 Multiply Monomials

Understand that polynomials form a system analogous to the integers, namely,
they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

Interpret expressions that represent a quantity in terms of its context.*

- Interpret parts of an expression, such as terms, factors, and coefficients.
- Interpret complicated expressions by viewing one or more of their parts as a single entity.

| Lesson | $\begin{array}{l}\text { Standards for an Algebra } 1 \text { Course } \\ \text { Multiply Monomials, } \\ \text { Binomials, and Trinomials }\end{array}$ | $\begin{array}{l}\text { Understand that polynomials form a system analogous to the integers, namely, } \\ \text { they are closed under the operations of addition, subtraction, and multiplication; } \\ \text { add, subtract, and multiply polynomials. } \\ \text { Interpret expressions that represent a quantity in terms of its context.* } \\ \text { - Interpret parts of an expression, such as terms, factors, and coefficients. } \\ \text { - Interpret complicated expressions by viewing one or more of their parts as a } \\ \text { single entity. }\end{array}$ | 2 days |
| :--- | :--- | :--- | :--- |$\}$


| 17.1 | Solve Quadratic Equations |
| ---: | :--- |
|  | by Graphing Quadratic |
|  | Functions | Functions

7.2 Solve Quadratic Equations by Factoring $x^{2}+b x+c$

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.*

- Graph linear and quadratic functions and show intercepts, maxima, and minima.

Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.*

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*

Solve quadratic equations in one variable.
2 days

- Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$.
Use the structure of an expression to identify ways to rewrite it.
Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.*

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*
Define appropriate quantities for the purpose of descriptive modeling.*
Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

|  | Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: | :---: |
| 17.3 | Solve Quadratic Equations by Factoring $a x^{2}+b x+c$ | Solve quadratic equations in one variable. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Use the structure of an expression to identify ways to rewrite it. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. | 2 days |
| 17.4 | Use Special Factoring Patterns to Solve Quadratic Equations | Solve quadratic equations in one variable. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Use the structure of an expression to identify ways to rewrite it. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. | 2 days |
| Module 18: Use Square Roots to Solve Quadratic Equations |  |  |  |
| 18.1 | Solve Quadratic Equations by Taking Square Roots | Solve quadratic equations in one variable. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.* | 2 days |


|  | Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: | :---: |
| 18.2 | Solve Quadratic Equations by Completing the Square | Solve quadratic equations in one variable. <br> - Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form $(x-p)^{2}=q$ that has the same solutions. Derive the quadratic formula from this form. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* | 2 days |
| 18.3 | Use the Quadratic Formula to Solve Equations | Solve quadratic equations in one variable. <br> - Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form $(x-p)^{2}=q$ that has the same solutions. Derive the quadratic formula from this form. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* <br> Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.* | 2 days |
| 18.4 | Choose a Method for <br> Solving Quadratic <br> Equations | Solve quadratic equations in one variable. <br> - Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.* | 1 day |

* This is also a modeling standard.


## Unit 9 FUNCTIONS AND MODELS

Module 19: Build Quadratic Functions and Models
19.1 Quadratic Functions in Vertex Form

Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.*

- Graph linear and quadratic functions and show intercepts, maxima, and minima.

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.*

Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*

Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.*

Write a function that describes a relationship between two quantities.*

- Determine an explicit expression, a recursive process, or steps for calculation from a context.

| Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: |
| 19.2 Quadratic Functions in Standard Form | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.* <br> - Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. <br> Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. <br> - Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

* This is also a modeling standard.

|  | Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: | :---: |
| 19.3 | Quadratic Functions in Intercept Form | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.* <br> - Factor a quadratic expression to reveal the zeros of the function it defines. <br> Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. <br> - Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| 19.4 | Compare Quadratic Functions | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <br> Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

## Pacing Guide

| Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: |
| 19.5 Scatter Plots and Fitted Quadratic Curves | Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.* <br> - Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

* This is also a modeling standard.

| 20.1 | Choose Among Linear, |
| :--- | :--- |
|  | Exponential, and Quadratic |
|  | Models |

Represent data on two quantitative variables on a scatter plot, and describe how
2 days the variables are related.*

- Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
Distinguish between situations that can be modeled with linear functions and with exponential functions.*
- Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
- Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.

Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.*

Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.*

Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.*

Define appropriate quantities for the purpose of descriptive modeling.*
Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*

Write a function that describes a relationship between two quantities.*

- Determine an explicit expression, a recursive process, or steps for calculation from a context.
20.2 Perform Operations with Functions

Write a function that describes a relationship between two quantities.*

- Combine standard function types using arithmetic operations.

Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
Write a function that describes a relationship between two quantities.*

- Determine an explicit expression, a recursive process, or steps for calculation from a context.

| Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: |
| 20.3 Solve Nonlinear Systems | Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. <br> Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.* <br> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.* <br> - Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> - Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude. <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |
| 20.4 Cubic Functions | Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial. <br> Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* <br> Define appropriate quantities for the purpose of descriptive modeling.* <br> Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. <br> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* <br> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.* <br> Write a function that describes a relationship between two quantities.* <br> - Determine an explicit expression, a recursive process, or steps for calculation from a context. | 2 days |

* This is also a modeling standard.

| Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: |
| Unit 10 DATA ANALYSIS |  |  |
| Module 21: Categorical Data |  |  |
| 21.1 Two-Way Frequency and Relative Frequency Tables | Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.* | 2 days |
| 21.2 Recognize Possible Associations Between Categorical Variables | Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.* | 2 days |


|  | Lesson | Standards for an Algebra 1 Course | Pacing |
| :---: | :---: | :---: | :---: |
| Module 22: Numerical Data |  |  |  |
| 22.1 | Data Distributions and Appropriate Statistics | Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.* <br> Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).* <br> Represent data with plots on the real number line (dot plots, histograms, and box plots).* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* | 2 days |
| 22.2 | Compare Data Distributions | Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.* <br> Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).* <br> Represent data with plots on the real number line (dot plots, histograms, and box plots).* <br> Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.* | 2 days |

* This is also a modeling standard.


[^0]:    * This is also a modeling standard.

