2 days

2 days

Apply and Practice

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Lesson	Mathematics Standards, Grade 7	Pacing
Unit 1 PROPORTIONAL RELATIONSHIPS		
Module 1: Identify and Represent Proport	ional Relationships	
Lesson 1.1 Explore Relationships	Recognize and represent proportional relationships between quantities.	1 day
	Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.	
Lesson 1.2 Recognize Proportional Relationships in Tables	Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.	2 days
	Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.	
	Represent proportional relationships by equations.	
Lesson 1.3 Compute Unit Rates Involving Fractions	Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.	2 days
Lesson 1.4 Recognize Proportional Relationships in Graphs	Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.	2 days
	Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.	
	Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points (0, 0) and (1, r) where r is the unit rate.	

relationships.

problems.

problems.

Identify the constant of proportionality (unit rate) in tables, graphs,

Use proportional relationships to solve multistep ratio and percent

including computing actual lengths and areas from a scale drawing and

Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.

Use proportional relationships to solve multistep ratio and percent

equations, diagrams, and verbal descriptions of proportional

Solve problems involving scale drawings of geometric figures,

reproducing a scale drawing at a different scale.



Lesson 1.5 Use Proportional

Problems

Lesson 1.6 Practice Proportional

Drawings

Reasoning with Scale

Relationships to Solve Rate

	Major
	Supporting
0	Additional

In addition to the core instructional pacing below, HMH recommends the following:

- 3 days per year for the HMH Into Math Growth Measure powered by Math Inventory
- 3 days per module for the Module Opener, Are You Ready?, Module Review, and Module Test
- 2 days per unit for the Performance Task

Using these recommendations, the total pacing for Grade 7 is 160 days.

Lesson	Mathematics Standards, Grade 7	Pacing	
Module 2: Proportional Reasoning with Percents			
Lesson 2.1 Percent Change	Use proportional relationships to solve multistep ratio and percent problems.	2 days	
Lesson 2.2 Markups and Discounts	Use proportional relationships to solve multistep ratio and percent problems.	2 days	
	Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.		
Lesson 2.3 Taxes and Gratuities	Use proportional relationships to solve multistep ratio and percent problems.	2 days	
Lesson 2.4 Commissions and Fees	Use proportional relationships to solve multistep ratio and percent problems.	2 days	
Lesson 2.5 Simple Interest	Use proportional relationships to solve multistep ratio and percent problems.	2 days	
Unit 2 RATIONAL NUMBER OPERATIONS			
Module 3: Understand Addition and Subtr	action of Rational Numbers		
Lesson 3.1 Add or Subtract a Positive Integer on a Number Line	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days	
	Understand $p + q$ as the number located a distance $ q $ from p , in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.		
Lesson 3.2 Add or Subtract a Negative Integer on a Number Line	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days	
	Understand $p+q$ as the number located a distance $ q $ from p , in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.		
Lesson 3.3 Use a Number Line to Add and Subtract Rational Numbers	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days	
	Describe situations in which opposite quantities combine to make 0.		
	Understand $p+q$ as the number located a distance $ q $ from p , in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.		

Apply and Practice

Lesson	Mathematics Standards, Grade 7	Pacing
Module 4: Add and Subtract Rational Nur	nbers	
Lesson 4.1 Compute Sums of Integers	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days
	Understand $p+q$ as the number located a distance $ q $ from p , in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.	
Lesson 4.2 Compute Differences of Integers	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days
	Understand subtraction of rational numbers as adding the additive inverse, $p-q=p+(-q)$. Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.	
Lesson 4.3 Compute Sums and Differences of Rational Numbers	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days
	Understand subtraction of rational numbers as adding the additive inverse, $p-q=p+(-q)$. Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.	
	Solve real-world and mathematical problems involving the four operations with rational numbers.	
Lesson 4.4 Apply Properties to Multi-step Addition and Subtraction Problems	Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line.	2 days
	Apply properties of operations as strategies to add and subtract rational numbers.	

	Lesson	Mathematics Standards, Grade 7	Pacing
Module 5:	Multiply and Divide Rational N	lumbers	
Lesson 5.1	Understand Multiplication and Division of Rational Numbers	 Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as (-1)(-1) = 1 and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts. Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers, then -(p/q) = (-p)/q = p/(-q). Interpret quotients of rational numbers by describing real-world contexts. 	2 days
		Apply properties of operations as strategies to multiply and divide rational numbers.	
Lesson 5.2	Multiply Rational Numbers	Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as $(-1)(-1) = 1$ and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.	1 day
		Apply properties of operations as strategies to multiply and divide rational numbers.	
		Solve real-world and mathematical problems involving the four operations with rational numbers.	
Lesson 5.3	Write Fractions as Decimals and Divide Integers	Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers, then $-\binom{p}{q} = \frac{(-p)}{q} = \frac{p}{(-q)}$. Interpret quotients of rational numbers by describing real-world contexts.	2 days
		Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats.	
		Solve real-world and mathematical problems involving the four operations with rational numbers.	
Lesson 5.4	Multiply and Divide Rational Numbers in Context	Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as $(-1)(-1) = 1$ and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.	1 day
		Solve real-world and mathematical problems involving the four operations with rational numbers.	
		Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	

Apply and Practice

Lesson	Mathematics Standards, Grade 7	Pacing
Module 6: Solve Multi-step Problems Usir	ng Rational Numbers	
Lesson 6.1 Apply Properties and Strategies to Operate with Rational Numbers	 Apply properties of operations as strategies to multiply and divide rational numbers. Solve real-world and mathematical problems involving the four 	1 day
	operations with rational numbers.	
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	
Lesson 6.2 Estimate to Check Reasonableness	Solve real-world and mathematical problems involving the four operations with rational numbers.	1 day
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	
Lesson 6.3 Solve Multi-step Problems with Rational Numbers in	Solve real-world and mathematical problems involving the four operations with rational numbers.	2 days
Context	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies	
	Use proportional relationships to solve multistep ratio and percent problems.	
Unit 3 MODEL WITH EXPRESSIONS, EQUA	ATIONS, AND INEQUALITIES	
Module 7: Solve Problems Using Expressi	ons and Equations	
Lesson 7.1 Write Linear Expressions in Different Forms for Situations	Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.	1 day
Lesson 7.2 Add, Subtract, and Factor Linear Expressions with	Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.	2 days
Rational Coefficients	Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.	

Lesson	Mathematics Standards, Grade 7	Pacing
Lesson 7.3 Write Two-step Equations for Situations	Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.	1 day
Lesson 7.4 Apply Two-step Equations to Solve Real-World Problems	Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where p , q , and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach.	2 days
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	
Lesson 7.5 Apply Two-Step Equations to Find Angle Measures	 Use facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure. 	2 days
	Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where p , q , and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach.	
Module 8: Solve Problems Using Inequali	ties	
Lesson 8.1 Understand and Apply Properties to Solve One-Step Inequalities	Solve word problems leading to inequalities of the form $px + q > r$ or $px + q < r$, where p, q , and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem.	2 days
Lesson 8.2 Write Two-Step Inequalities for Situations	Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.	2 days
Lesson 8.3 Apply Two-Step Inequalities to Solve Problems	Solve word problems leading to inequalities of the form $px + q > r$ or $px + q < r$, where p , q , and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem.	2 days

Apply and Practice

Lesson	Mathematics Standards, Grade 7	Pacing
Unit 4 GEOMETRY		
Module 9: Draw and Analyze Two-Dimens	sional Figures	
Lesson 9.1 Draw Circles and Other Figures	Oraw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.	2 days
Lesson 9.2 Draw and Construct Triangles Given Side Lengths	Oraw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.	2 days
Lesson 9.3 Draw and Construct Triangles Given Angle Measures	Oraw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.	2 days
Lesson 9.4 Draw and Analyze Shapes to Solve Problems	Oraw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.	1 day
Module 10: Analyze Figures to Find Circu	imference and Area	
Lesson 10.1 Derive and Apply Formulas for Circumference	Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.	1 day
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	
Lesson 10.2 Derive and Apply a Formula for the Area of a Circle	Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.	2 days
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	

Lesson	Mathematics Standards, Grade 7	Pacing
Lesson 10.3 Describe and Analyze Cross Sections of Circular Solids	 Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. 	2 days
Lesson 10.4 Areas of Composite Figures	 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. 	1 day
Module 11: Analyze Surface Area and Vo	lume	
Lesson 11.1 Describe and Analyze Cross Sections of Prisms and Pyramids	 Describe the two-dimensional figures that result from slicing three- dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. 	1 day
Lesson 11.2 Derive and Apply Formulas for Surface Areas of Cubes and Right Prisms	 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. 	1 day
Lesson 11.3 Derive and Apply a Formula for the Volume of a Right Prism	 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. 	1 day

Lesson	Mathematics Standards, Grade 7	Pacing
Module 11: Analyze Surface Area and Vo	lume	
Lesson 11.4 Solve Multi-step Problems with Surface Area and Volume	 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. 	2 days
Unit 5 SAMPLING AND DATA ANALYSIS		
Module 12: Proportional Reasoning with	Samples	
Lesson 12.1 Understand Representative Samples	Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid inferences.	1 day
Lesson 12.2 Make Inferences from a Random Sample	Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.	2 days
Lesson 12.3 Make Inferences from Repeated Random Samples	Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.	1 day
Module 13: Use Statistics and Graphs to C	ompare Data	
Lesson 13.1 Compare Center and Spread of Data Displayed in Dot Plots	 Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. 	1 day
Lesson 13.2 Compare Center and Spread of Data Displayed in Box Plots	 Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. 	1 day
Lesson 13.3 Compare Means Using Mean Absolute Deviation and Repeated Sampling	 Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. 	2 days

Lesson	Mathematics Standards, Grade 7	Pacing
Unit 6 PROBABILITY		
Module 14: Understand and Apply Experi	mental Probability	
Lesson 14.1 Understand Probability of an Event	Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near 0 indicates an unlikely event, a probability around $\frac{1}{2}$ indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event.	1 day
Lesson 14.2 Find Experimental Probability of Simple Events	Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.	2 days
	Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.	
	Use proportional relationships to solve multistep ratio and percent problems.	
Lesson 14.3 Find Experimental Probability of Compound Events	Understand that, just as with simple events, the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs.	2 days
	Represent sample spaces for compound events using methods such as organized lists, tables and tree diagrams. For an event described in everyday language (e.g., "rolling double sixes"), identify the outcomes in the sample space which compose the event.	
	Use proportional relationships to solve multistep ratio and percent problems.	
Lesson 14.4 Use Experimental Probability and Proportional Reasoning to Make Predictions	Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.	2 days
	Use proportional relationships to solve multistep ratio and percent problems.	
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	

Lesson	Mathematics Standards, Grade 7	Pacing
Module 15: Understand and Apply Theor	retical Probability	
Lesson 15.1 Find Theoretical Probability of Simple Events	Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.	2 days
	Develop a probability model and use it to find probabilities of events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.	
	Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events.	
	Use proportional relationships to solve multistep ratio and percent problems.	
Lesson 15.2 Find Theoretical Probability of Compound Events	Understand that, just as with simple events, the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs.	2 days
	Represent sample spaces for compound events using methods such as organized lists, tables and tree diagrams. For an event described in everyday language (e.g., "rolling double sixes"), identify the outcomes in the sample space which compose the event.	
	Use proportional relationships to solve multistep ratio and percent problems.	
Lesson 15.3 Use Theoretical Probability and Proportional Reasoning to Make Predictions	Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.	2 days
	Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events.	
	Use proportional relationships to solve multistep ratio and percent problems.	
	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.	
Lesson 15.4 Conduct Simulations	Design and use a simulation to generate frequencies for compound events.	2 days
	Use proportional relationships to solve multistep ratio and percent problems.	